

Problem Set 12  
Due in lecture Thursday, December 6

1. Romer, Problem 10.12.

(From an old final.) 2. In the Diamond-Dybvig model, the key departure from Walrasian assumptions is:

- A. Asymmetric information between entrepreneurs and outside investors.
- B. The presence of noise traders.
- C. Preference shocks.
- D. The lack of observability of agents' types.

(From the Fall 2016 final.) 3. In the Delong-Shleifer-Summers-Waldmann model, noise traders increase the volatility of the price of an asset by:

- A. Increasing the variance of the demand for the asset, thereby causing fluctuations in its price.
- B. Making the return on the asset riskier, thereby making the demand of rational traders for the asset less responsive to its price.
- C. Increasing the variance of shocks to the fundamental value of the asset.
- D. (A) and (B).
- E. All of the above.
- F. None of the above.

(Based on a problem on the Fall 2016 final.) 4. Two of the subsection titles in "What Explains the 2007–2009 Drop in Employment?" by Atif Mian and Amir Sufi are:

- A. "Cosyndication and the Elasticity of Housing Supply" and "Sensitivity to the Sand States."
- B. "The Elasticity of Substitution between Goods Produced Locally and Elsewhere" and "Sensitivity to Measurement Error."
- C. "The Frisch Elasticity of Labor Supply" and "Implications for Fiscal Policy."
- D. "The Business Uncertainty Hypothesis" and "Supply-Side Sector-Specific Shocks."

EXTRA PROBLEMS (NOT TO BE HANDED IN; COMPLETE ANSWERS MAY NOT BE PROVIDED)

5–8. Romer, Problems 10.7, 10.8, 10.9, and 10.11. (Note: in part (a) of Problem 10.11, " $c_1^{b*}$ " should be " $c_2^{b*}$ ".)

(From the Fall 2016 final.) 9. A researcher is interested in studying the impact of bank failures on economic activity. They are concerned about reverse causation, so they look at the relation between bank failures in period  $t - 1$  and growth in period  $t$ . Specifically, they estimate, using OLS, the regression:

$$\Delta y_t = a + bF_{t-1} + e_t,$$

where  $\Delta y_t$  is the change in log real GDP from period  $t - 1$  to period  $t$  and  $F_{t-1}$  is a measure of bank failures in period  $t - 1$ .

Is this regression a good way to get an estimate of the causal effect of bank failures on GDP? Explain your answer.

10. (This follows Jacklin, 1987.) Consider the Diamond-Dybvig model as presented in lecture and in the reading. But suppose that instead of a bank, there is a firm. The firm obtains  $S$  units of the economy's endowment by selling  $S$  shares in period 0 (the price of a share in units of period 0 endowment is 1). The firm's business plan (to which it is committed) is to invest the  $S$  units; pay a dividend of  $D_1$  per share in period 1 (by liquidating fraction  $D_1$  of its investment); and then pay a dividend of  $D_2$  per share in period 2 that leaves it with no remaining assets.

- a. Explain why  $D_2 = R(1 - D_1)$ .
- b. Suppose all agents use their endowment to buy shares in the firm, and suppose there is a market for shares in the firm in period 1 after  $D_1$  has been paid. If all type a agents sell their shares and all type b agents use all of their period 1 dividends to buy shares, what will the price of shares,  $P$ , be as a function of  $D_1$  and  $\theta$ ?
- c. Continue to assume that all type a agents sell their shares and all type b agents use all of their period 1 dividends to buy shares. What will be the consumption of type a agents in period 1? The consumption of type b agents in period 2?
- d. Is there a value of  $D_1$  that yields the social optimum? Explain. (Recall that the social optimum is for the type a agents to consume  $1/[\theta + (1 - \theta)\rho]$  in period 1 and for the type b's to consume  $\rho R/[\theta + (1 - \theta)\rho]$  in period b.)
- e. For what values of  $P$  will the type a agents want to sell their shares (or be indifferent)? For what values of  $P$  will the type b agents want to buy shares (or be indifferent)? With  $D_1$  equal to the value you found in part (d), are these conditions satisfied?
- f. Is this equilibrium vulnerable to a run? Explain.

(From the Fall 2016 final.) 11. This problem asks you to sketch how you would go about analyzing a variant of the Diamond-Dybvig model. (**Note: The problem does NOT ask you to solve the model. You will receive no extra credit for doing more than the problem asks you to do.**)

Consider the usual Diamond-Dybvig model. The key difference is that  $\theta$  – the fraction of agents who learn in period 1 that they are type  $a$  – is random. It can take on two values,  $\theta_L$  and  $\theta_H$  ( $0 < \theta_L < \theta_H < 1$ ), each with probability one-half. The realization of  $\theta$  is not observable.

The other assumptions are the same. Briefly: Agents live for 3 periods. Ex ante, they are identical. Those who turn out to be type  $a$  have utility  $\ln c_1^a$ , and those who turn out to be type  $b$  have utility  $U^b = \rho \ln(c_1^b + c_2^b)$ ,  $0 < \rho < 1$ . Each agent is endowed with 1 unit of the economy's good in period 0. The unit yields 1 unit if it is consumed in period 1, and  $R > 1$  units if it is consumed in period 2. The model assumes  $\rho R > 1$ .

a. Sketch how you would find the first-best, full-information allocation (that is, the consumption of each type of agent in each period as a function of  $\theta$  if individuals' types and the realization of  $\theta$  were observable).

b. Consider a bank as in the standard Diamond-Dybvig model. The bank offers a contract of the following form. If an individual deposits their endowment with the bank, they can withdraw some amount  $X$  in period 1; in period 2, the bank's remaining assets are divided equally among all depositors who did not withdraw in period 1. If the bank does not have enough resources to pay  $X$  to everyone who wants to withdraw in period 1, a subset of the early withdrawers, chosen at random, get  $X$  so that the bank's resources are exhausted, and the remaining depositors get nothing.

Explain why if fraction  $f$  of depositors withdraw in period 1, the amount each depositor who waits until period 2 receives is  $\max\{(1 - fX)R/(1 - f), 0\}$ .

c. What condition must  $X$  satisfy for it to be a Nash equilibrium for the type  $a$ 's, and only the type  $a$ 's, to always withdraw in period 1? For simplicity, call this a "good Nash equilibrium".

d. Assume that if a good Nash equilibrium exists, then it is the outcome. Set up, but do not solve, the problem of finding the best good Nash equilibrium – that is, the value of  $X$  for which the good Nash equilibrium gives the highest expected utility of the representative agent before they know their type or the realization of  $\theta$ .

e. Suppose you wanted to analyze the question of whether for some value of  $X$  where there is a good Nash equilibrium, a bank run is also a Nash equilibrium. Sketch how you would go about doing that.

f. Suppose you wanted to analyze the question of whether there is some value of  $X$  for which there is a good Nash equilibrium and that equilibrium achieves the first-best allocation discussed in part (a). Sketch how you would go about doing that.